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Modeling of spin metal-oxide-semiconductor field-effect transistor: A nonequilibrium Green's function approach with spin relaxation

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(Received 10 July 2008; accepted 19 September 2008; published online 12 November 2008)

A spin metal-oxide-semiconductor field-effect transistor (spin MOSFET), which combines a Schottky-barrier MOSFET with ferromagnetic source and drain contacts, is a promising device for spintronic logic. Previous simulation studies predict that this device should display a very high magnetoresistance (MR) ratio (between the cases of parallel and antiparallel magnetizations) for the case of half-metal ferromagnets (HMF). We use the nonequilibrium Green's function formalism to describe tunneling and carrier transport in this device and to incorporate spin relaxation at the HMF-semiconductor interfaces. Spin relaxation at interfaces results in nonideal spin injection. Minority spin currents arise and dominate the leakage current for antiparallel magnetizations. This reduces the MR ratio and sets a practical limit for spin MOSFET performance. We found that MR saturates at a lower value for smaller source-to-drain bias. In addition, spin relaxation at the detector side is found to be more detrimental to MR than that at the injector side, for drain bias less than the energy difference of the minority spin edge and the Fermi level. © 2008 American Institute of Physics. [DOI: 10.1063/1.3013438]

I. INTRODUCTION

In recent years, a vigorous research effort to demonstrate spintronic devices^{1,2} has been pursued. One of the motivations has been that spin-based devices are identified as one of the most promising alternatives to traditional charge-based logic devices by the International Technology Roadmap for Semiconductors.³ Simulations have predicted that spintronic logic can scale in its size with smaller switching energy and less overall power dissipation than electronic logic.⁴

The concept and operating principles of the first magnetic three-terminal device, i.e., the spin current modulator, was proposed by Datta and Das⁵ in 1990. It comprises of a gate controlling the spin precession in a semiconductor channel, a ferromagnetic (FM) source injecting highly polarized spins, and a FM drain detecting the spin polarization. The current depends both on the relative directions of magnetization of the source and the drain and on the gate bias. Without the gate field, the spin current modulator can act as a giant magnetoresistance (MR) device.⁶ The gate exerts an effective magnetic field (Rashba field),^{7,8} which causes precession of the spins as they move along the channel. With enough channel length and strong enough Rashba field, the angle of spin precession can be varied from 0 or π , generating the device ON and OFF states, respectively, for parallel magnetizations. Since the device operation involves a precise phase of the spins, it is desirable to suppress any scattering mechanisms, i.e., the device works best at low temperature and in samples with few defects. Physical realization of the Datta–Das spin current modulator is mainly impeded by the substantial difficulties of obtaining efficient room-temperature spin injection

from the FM contacts into the semiconductors such as GaAs (Ref. 9) and Si.¹⁰ A recent realization of spin field effect transistor¹¹ (FET) using hot-electron transport through FM thin films for all-electrical spin polarized injection and detection¹² with a Si channel is encouraging. There the electric field controls the transit time of electrons and thus its precession in the magnetic field. However, it seems unlikely that the Datta–Das spin current modulator or any other spin precession devices can provide the ON/OFF current ratio comparable to traditional electronic metal-oxide-semiconductor FETs (MOSFETs).

Another type of a spin transistor, a spin MOSFET, was proposed by Sugahara and Tanaka.¹³ It is in essence a Schottky barrier (SB) MOSFET, where the source and drain are FM. A half-metal ferromagnet (HMF) was employed in the original proposal, i.e., a material having 100% of electrons with one direction of spin at its Fermi level.¹⁴ This property is conducive to higher spin polarization of injected carriers. Silicon's mature technology base makes it a preferred choice for a channel material. Furthermore, the low spin relaxation rate due to its relatively small spin-orbit effects and negligible hyperfine interaction gives propagating electrons in Si a substantially long spin lifetimes.¹⁵ The authors of Ref. 13 argued that spin MOSFETs might be used for high-density nonvolatile memory, whose cell contains a single spin transistor, as well as for nonvolatile, reconfigurable logic circuits.¹⁶ The difference between the spin MOSFET and a spin current modulator is that the former does not rely on the phase of the spin precession. Instead, the current is controlled by the height of the SBs, which is different for electrons with different spins. This is due to the fact that the states of electrons with spin along and opposite to the magnetization are split by the value of the exchange

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interaction in the ferromagnet. The role of the gate is to change the electrical potential and thus the thickness of the SBs. Together the directions of magnetization and the gate bias determine the current through the transistor.

In all types of spin transistors, the key device metric is the MR ratio, i.e., the ratio of currents for parallel and anti-parallel magnetizations. It is a measure of the control of carrier transport by the magnetic state of the device. Theoretically, HMFs will have 100% spin polarization (all the spins being aligned with the magnetization) as first predicted by density functional theory for NiMnSb (Ref. 14) and also supported by experiments such as spin-resolved positron annihilation¹⁷ and infrared reflectance spectroscopy.¹⁸ Therefore, one expects injection of 100% spin polarized carriers from a HMF source, which would lead to an extremely large MR ratio in the spin MOSFET.¹³ The class of Heusler alloys of type X-MnSb are excellent candidates for HFM.¹⁹ Genuine half-metallic interfaces of NiMnSb with III-V semiconductors (e.g., InP and CdS) were predicted in the [111] direction with both HMF and semiconductor being anion terminated at the interface.²⁰ Alternatively, one could also consider nonmagnetic semiconducting Heusler alloys (e.g., NiMnSb, NiScSb, NiTiSn, and CoTiSb), which provide a smaller lattice mismatch with Heusler type HMF. Of particular importance is CoTiSb, a semiconductor with indirect bandgap with conduction energy minimum along the sixfold degenerate Γ_X symmetry lines, just like Si.²¹

However, high spin polarization of injected carriers has not yet been achieved with HMF. Experiments on spin-polarized photoemission²² and spin-polarized tunneling²³ with HMF result in spin polarization values far below 100%. This is attributed to the presence of a “magnetically dead layer,” i.e., an area close to the surface of the FM which is not FM. Its random magnetization interacts with the spins of injected carriers and thus decreases their spin polarization. In particular, a recent first-principle study of half-metallic NiMnSb/CdS interface reveals that the NiMnSb surfaces are not half-metallic, even if they are stoichiometric and perfectly ordered.²⁰ Therefore, in order to estimate a realistic performance of spin MOSFET, one has to take into account spin relaxation processes at these interfaces.

Many publications have addressed the simulation of spin-dependent transport. The drift-diffusion approach to spin transport with spin flip processes is reviewed in Ref. 24. However, quantum tunneling processes cannot be handled by this method. The quantum conductance treatment had been applied²⁵ to simulation of a spin-flip transistor. Nonequilibrium Green's function (NEGF) treatment of tunneling in FM metal-oxide multilayers with spin relaxation was described in Refs. 26 and 27. NEGF has also been applied to spin transport in carbon nanotubes²⁸ and molecules.²⁹ The contribution of our work is to treat quantum transport through metal and semiconductor structures with spin relaxation at the interfaces and under the influence of a self-consistent electrostatic field.

In this paper, we describe a full quantum-mechanical model for simulating carrier transport in a spin MOSFET, based on the Keldysh NEGF approach.^{30–32} In our model, we capture the physics of carrier injection and extraction, tun-

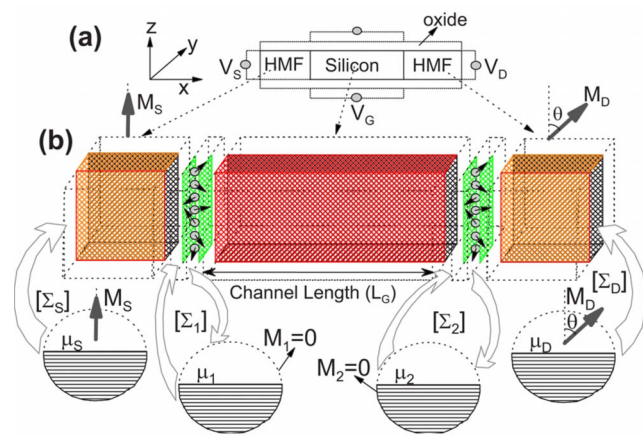


FIG. 1. (Color online) (a) A schematic illustration of the three terminal (i.e., gate contact V_G , drain contact V_D and source contact V_S) spin MOSFET device. A double-gate structure is employed. (b) A zoom-in illustration of the supercell used for the construction of device Hamiltonian depicting the various self-energies used in the calculation.

neling through SBs, quantum interference of electron wave reflections, and spin relaxation. The influence of the magnetically dead layer is incorporated via a scattering self-energy of interaction of spin of carriers and localized electrons, derived within the self-consistent Born approximation.^{26,33} We quantify the effects of spin relaxation on the MR ratio of the spin MOSFET. The rest of this paper is organized as follows. In Sec. II, we introduce the NEGF formalism with a detailed mathematical description of the physical quantities used in the formalism. In Sec. III, we apply this approach to the study of spin MOSFET in the coherent regime (without spin relaxation). The bias dependence of MR ratio is explained in this section. In Sec. IV, we examine the effect of the magnetically dead layer on spin transport in spin MOSFET. In Sec. V, we explore the dependence of the MR ratio on the strength of interaction with a magnetically dead layer. Conclusions are drawn in Sec. VI. In Appendix A, we present a derivation of the scattering self energy within the self-consistent Born approximation. In Appendix B, a simple ohmic model analysis of spin MOSFET with HMF and FM source/drain contacts is discussed.

II. MODEL DESCRIPTION

A schematic drawing of a spin MOSFET is illustrated in Fig. 1. We employed here a double-gate structure with a thin film semiconductor for which the gate control of electrostatics is optimal. The channel is a semiconductor and the source/drain contacts are HMFs (Ref. 21) with magnetization of \mathbf{M}_S and \mathbf{M}_D , respectively. The device is large in the y direction. Therefore Fig. 1 depicts the supercell for our transport problem, where the wavefunction solution repeats periodically in the y direction. We employ the effective mass approach to the description of the bandstructure. The Hamiltonian and the Schrödinger equation reduce to the following Sturm–Liouville problem in the longitudinal plane [$\mathbf{r} = (x, z)$] (omitting the spin relaxation terms here),

$$H\Psi_{\sigma}(\mathbf{r}) = -\frac{\hbar^2}{2}\nabla_r[M^{-1}(\mathbf{r})\nabla_r\Psi(\mathbf{r})] + [V(\mathbf{r}) + \epsilon_y + \mathbf{M}(\mathbf{r})\sigma]\Psi_{\sigma}(\mathbf{r}) = \epsilon\Psi_{\sigma}(\mathbf{r}), \quad (1)$$

where $M^{-1}(\mathbf{r})$ is the effective mass tensor, with diagonal elements m_x^{-1} and m_z^{-1} .³⁴ We assume that the transport mass (m_x), transverse mass (m_y), and quantization mass (m_z) are spatially uniform within each material. $\mathbf{M}(\mathbf{r})$ is the magnetization at \mathbf{r} , $\sigma=(\sigma_x, \sigma_y, \sigma_z)$ are the Pauli spin matrices, and $\nabla_r \equiv \partial_x \mathbf{i} + \partial_z \mathbf{k}$. The eigenvalue of H is the total energy ϵ , while $\epsilon_y = \hbar^2 k_y^2 / 2m_y$ is the transverse energy corresponding to the transverse mode solution $\phi(y) = \exp(ik_y y) / \sqrt{w}$. In this work, we use the finite difference approach to express our physical quantities in matrix representation.³⁰ Assuming that the electrostatic potential is separable, i.e., can be represented as $V(\mathbf{r}) \approx V_1(x) + V_2(z)$, we can further reduce our system Eq. (1) to a one-dimensional problem.³⁵

The Keldysh NEGF approach³⁰⁻³² is a powerful technique in solving electronic transport in nanostructures having open boundary conditions. The infinite problem domain (Ω) which consists of the semiconductor channel and two semi-infinite HMF leads is partitioned into an exterior (Ω_e) and an interior domain (Ω_i), where only the solutions within Ω_i is to be sought. In this work, Ω_i is composed of the semiconductor channel and a small segment of the HMF at the source/drain. In the absence of scattering, the Green's function G in Ω_i is written as

$$G(\epsilon_x) = [(\epsilon_x)I - H - V_1 - \Sigma_c(\epsilon_x)]^{-1}, \quad (2)$$

where $\Sigma_c = \Sigma_L + \Sigma_R$ is the contacts self-energy³⁰ and $\epsilon_x = \epsilon - \epsilon_y - \epsilon_j$ with ϵ_j being the subband energy of the j th mode due to the z confinement. For a one-dimensional lattice with a nearest neighbor coupling energy of t and lattice spacing of a , the contact self-energy is written as

$$\begin{bmatrix} c_i & s_i \\ -s_i & c_i \end{bmatrix} \begin{bmatrix} -te^{ik_i^{\dagger}a} & 0 \\ 0 & -te^{ik_i^{\dagger}a} \end{bmatrix} \begin{bmatrix} c_i & s_i \\ -s_i & c_i \end{bmatrix}^{\dagger}, \quad (3)$$

where $c_i = \cos(\theta_i/2)$, $s_i = \sin(\theta_i/2)$, i labels the left (source) and right (drain) contacts (i.e., $i=L, R$), and θ_i is the magnetization angle with respect to z -axis. We will designate the majority spin as “spin up” and the minority spins as “spin down.” $k_i^{\dagger} = [2m_x(\epsilon - \epsilon_y - \epsilon_j - E_i^{\dagger})]^{1/2}/\hbar$ is the wave vector in the contact i , and the energy of the majority band edge is E_i^{\dagger} . A similar identity holds for k_i^{\dagger} and E_i^{\dagger} . The difference between the energies of the minority and the majority spin band edges is the exchange splitting in the ferromagnet $\Delta_s = E_i^{\dagger} - E_i^{\dagger}$. The Fermi energy (equivalently, the electrochemical potential) in contact i is designated ϵ_F^i . The energy bandwidth of occupied states in HMF is defined as $E_w = \epsilon_F^i - E_i^{\dagger}$, where E_i^{\dagger} is the energy of the majority spin band.

In the ballistic case, states in the device are filled and emptied through the contacts. Conventionally, they can be

defined as the filling and emptying functions (analogous to the inscattering and outscattering functions in the case of scattering³⁰),

$$\begin{aligned} \Sigma_i^{\text{in}}(\epsilon_x)|_{\epsilon_y, \epsilon_j} &= f_0(\epsilon_x + \epsilon_y + \epsilon_j - \epsilon_F^i)\Gamma_i(\epsilon_x), \\ \Sigma_i^{\text{out}}(\epsilon_x)|_{\epsilon_y, \epsilon_j} &= [1 - f_0(\epsilon_x + \epsilon_y + \epsilon_j - \epsilon_F^i)]\Gamma_i(\epsilon_x), \end{aligned} \quad (4)$$

where $\Gamma_i = i[\Sigma_i - \Sigma_i^{\dagger}]$ is the broadening functions of the respective contact $i=L, R$. The electron and hole correlation functions are defined as

$$G^{n,p}(\epsilon_x)|_{\epsilon_y, \epsilon_j} = G(\epsilon_x)\Sigma_c^{\text{in,out}}(\epsilon_x)|_{\epsilon_y, \epsilon_j}G(\epsilon_x)^{\dagger}, \quad (5)$$

where $\Sigma_c^{\text{in,out}} = \Sigma_L^{\text{in,out}} + \Sigma_R^{\text{in,out}}$. The transverse modes can be summed over, and we obtain the aggregated electron correlation function \tilde{G}^n ,

$$\tilde{G}^n(\epsilon_x) = G(\epsilon_x)\tilde{\Sigma}_c^{\text{in}}(\epsilon_x)G(\epsilon_x)^{\dagger}, \quad (6)$$

with the aggregated filling function defined as

$$\tilde{\Sigma}_c^{\text{in}}(\epsilon_x) = \sum_j F(\epsilon_x + \epsilon_j - \epsilon_F^i)\Gamma_i(\epsilon_x), \quad (7)$$

where $F(\epsilon_x + \epsilon_j - \epsilon_F^i)$ is the Fermi Dirac integral of order $-\frac{1}{2}$.³⁶ The diagonal elements of $\tilde{G}^n(\epsilon_x)$ are related to the charge spectral density at energy ϵ_x . Once the total charge density is evaluated, the electrostatic potential V_1 can be obtained using Poisson equation self-consistently.

To include the effect of spin relaxation, we have to modify the Green's function in Eq. (2). Spin relaxation processes arise from the interaction of spins of free carriers with the spins of localized electrons, e.g., in the magnetically dead layer. The Heisenberg Hamiltonian for the spin interaction is

$$H_I = J_{\mathbf{S}} \cdot \mathbf{S}, \quad (8)$$

where the spin operators for free electrons are \mathbf{s} and those for localized electrons are \mathbf{S} , all in units of \hbar . For spin=1/2, these operators are related to the Pauli matrices $\mathbf{s} = \sigma/2$. The interaction energy is given by J .

Assuming that the localized electrons are numerous, they thus form a reservoir causing an incoherent evolution of the free carrier spins. The state of the reservoir is described by its density matrix. For the case of spin=1/2 reservoir, it has the form

$$\rho = \begin{pmatrix} F_u & \Delta \\ \Delta^* & F_d \end{pmatrix}, \quad (9)$$

where the spin-up and spin-down occupation numbers are F_u and F_d (such that $F_u + F_d = 1$).

In this paper, we assume that spin relaxation processes are elastic (do not change the energy of free carriers). In the self-consistent Born approximation,³² one can express the in- and outscattering self-energy as a function of the electron and hole correlation functions,^{26,33}

$$\begin{aligned} \Sigma_{s,ij}^{\text{in}}(\epsilon) &= \gamma(\epsilon)\Phi_{ijkl}^n G_{kl}^n(\epsilon), \\ \Sigma_{s,ij}^{\text{out}}(\epsilon) &= \gamma(\epsilon)\Phi_{ijkl}^p G_{kl}^n(\epsilon), \end{aligned} \quad (10)$$

where $\gamma(\epsilon)$ is the quantity with the dimension of energy-squared proportional to the relaxation rate, which depends on

the number of localized spins and the interaction energy, $\Phi^{n/p}$ are the four-index tensors which provides a mapping between electron/hole correlation functions with the in/outscattering functions. They are products of spin operators

and the reservoir density matrix (9). Their specific form and derivations are provided in Appendix A.

In the case of spin=1/2 reservoir and diagonal density matrix ($\Delta=0$), the explicit form can be derived

$$\begin{aligned} \Sigma_s^{\text{in}}(\epsilon_x)|_{\epsilon_y, \epsilon_j} &= \gamma(\epsilon_x) \begin{bmatrix} F_u G_{\downarrow\downarrow}^n(\epsilon_x) + \frac{1}{4} G_{\uparrow\uparrow}^n(\epsilon_x) & -\frac{1}{4} G_{\uparrow\downarrow}^n(\epsilon_x) \\ -\frac{1}{4} G_{\downarrow\uparrow}^n(\epsilon_x) & F_d G_{\uparrow\uparrow}^n(\epsilon_x) + \frac{1}{4} G_{\downarrow\downarrow}^n(\epsilon_x) \end{bmatrix}_{\epsilon_y, \epsilon_j}, \\ \Sigma_s^{\text{out}}(\epsilon_x)|_{\epsilon_y, \epsilon_j} &= \gamma(\epsilon_x) \begin{bmatrix} F_d G_{\downarrow\downarrow}^p(\epsilon_x) + \frac{1}{4} G_{\uparrow\uparrow}^p(\epsilon_x) & -\frac{1}{4} G_{\uparrow\downarrow}^p(\epsilon_x) \\ -\frac{1}{4} G_{\downarrow\uparrow}^p(\epsilon_x) & F_u G_{\uparrow\uparrow}^p(\epsilon_x) + \frac{1}{4} G_{\downarrow\downarrow}^p(\epsilon_x) \end{bmatrix}_{\epsilon_y, \epsilon_j}. \end{aligned} \quad (11)$$

The broadening function due to scattering is given by

$$\Gamma_s(\epsilon_x)|_{\epsilon_y, \epsilon_j} = [\Sigma_s^{\text{in}}(\epsilon_x)|_{\epsilon_y, \epsilon_j} + \Sigma_s^{\text{out}}(\epsilon_x)|_{\epsilon_y, \epsilon_j}]. \quad (12)$$

If we assumed there is no coupling between the different ϵ_y and ϵ_j modes,

$$\Sigma_s^{\text{out}}(\epsilon_x)|_{\epsilon_y, \epsilon_j} = \frac{1}{2\pi} \int \frac{\Gamma_s(\epsilon_x)|_{\epsilon_y, \epsilon_j}}{\epsilon'_x - \epsilon_x} d\epsilon'_x - i \frac{\Gamma_s(\epsilon_x)|_{\epsilon_y, \epsilon_j}}{2}. \quad (13)$$

The noncoherent Green's function for a particular transverse mode (ϵ_y, ϵ_j) is given by

$$G(\epsilon_x)|_{\epsilon_y, \epsilon_j} = [(\epsilon_x)I - H - V_1 - \Sigma_c(\epsilon_x) - \Sigma_s(\epsilon_x)|_{\epsilon_y, \epsilon_j}]^{-1}, \quad (14)$$

whereas the electron and hole correlation functions are defined as

$$\begin{aligned} G^{n,p}(\epsilon_x)|_{\epsilon_y, \epsilon_j} &= G(\epsilon_x) [\Sigma_c^{\text{in,out}}(\epsilon_x)|_{\epsilon_y, \epsilon_j} \\ &+ \Sigma_s^{\text{in,out}}(\epsilon_x)|_{\epsilon_y, \epsilon_j}] G(\epsilon_x)^\dagger. \end{aligned} \quad (15)$$

The solutions are sought by solving the set of functions $\Sigma_s(\epsilon_x)|_{\epsilon_y, \epsilon_j}$, $G^{n,p}(\epsilon_x)|_{\epsilon_y, \epsilon_j}$ and $G(\epsilon_x)|_{\epsilon_y, \epsilon_j}$ self-consistently for each energy ϵ_x and modes (ϵ_y, ϵ_j). This iterative process makes it numerically prohibitive to solving realistic transport problems.

In this work, we shall introduce some simplifications to make the numerics more tractable. First, we assumed that the relaxation rate γ is energy independent. Under the condition where the impurity spin state is uncorrelated and with equal up and down spin occupation probability, i.e., $F_u = F_d = \frac{1}{2}$, it can also be shown that the function $\Phi^n = \Phi^p = \Phi$.²⁶ Henceforth, the broadening due to scattering is given by

$$\Gamma_s(\epsilon_x)|_{\epsilon_y, \epsilon_j} = \gamma \Phi A(\epsilon_x) \equiv \Gamma_s(\epsilon_x),$$

where A is the local density of state

$$A(\epsilon_x) = i[G(\epsilon_x) - G(\epsilon_x)^\dagger] = G^n(\epsilon_x) + G^p(\epsilon_x). \quad (16)$$

We had assumed in Eq. (16) that the local density of states for each transverse modes (ϵ_y, ϵ_j) is the same and is only dependent on the longitudinal energy ϵ_x . Similarly, the scattering self energy $\Sigma_s(\epsilon_x)$ [computed using Eq. (13)] and Green's function $G(\epsilon_x)$ are modes independent. The aggregated electron correlation function can then be computed self-consistently from

$$\tilde{G}^n(\epsilon_x) = G(\epsilon_x) [\tilde{\Sigma}_s^{\text{in}}(\epsilon_x) + \tilde{\Sigma}_c^{\text{in}}(\epsilon_x)] G(\epsilon_x)^\dagger, \quad (17)$$

where the aggregated inscattering self-energy for a spin $\frac{1}{2}$ impurity is written as

$$\begin{aligned} \tilde{\Sigma}_s^{\text{in}}(\epsilon_x) &= \gamma \begin{bmatrix} F_u G_{\downarrow\downarrow}^n(\epsilon_x) + \frac{1}{4} G_{\uparrow\uparrow}^n(\epsilon_x) & -\frac{1}{4} G_{\uparrow\downarrow}^n(\epsilon_x) \\ -\frac{1}{4} G_{\downarrow\uparrow}^n(\epsilon_x) & F_d G_{\uparrow\uparrow}^n(\epsilon_x) + \frac{1}{4} G_{\downarrow\downarrow}^n(\epsilon_x) \end{bmatrix}. \end{aligned} \quad (18)$$

The scattering strength of a layer of impurities is defined by the product γa , where a is the lattice spacing, which physically speaking is the thickness of the interfacial layer in our study. Current is calculated from the self-consistent solution of the above equations for any terminal i ,

$$I_i = \int_{-\infty}^{\infty} I(\epsilon_x) d\epsilon_x, \quad (19)$$

where $I(\epsilon_x)$ is defined as

$$I(\epsilon_x) = \frac{q}{h} \text{Tr}[\tilde{\Sigma}_i^{\text{in}}(\epsilon_x) A(\epsilon_x) - \Gamma_i(\epsilon_x) \tilde{G}^n(\epsilon_x)]. \quad (20)$$

The formalism described in this section allows us to combine the description of quantum transport in the device with the incoherent processes of spin relaxation.

III. SPIN-MOSFET: COHERENT REGIME

We consider a spin MOSFET with a double-gated structure, as depicted in Fig. 1 with a 3 nm thin film Si channel. The channel length is 12 nm with gate oxide thickness of 1 nm. Due to the strong body confinement, electrons predominantly occupy the doubly degenerate valleys along $\mathbf{k} = (0, 0, 1)$. Its energy dispersion can be described within the effective mass approximation with a longitudinal mass of $0.91m_0$ (m_z) and a transverse mass of $0.91m_0$ (m_x, m_y). HMFs are employed for the source and drain contacts.

Despite optimistic theoretical projections, engineering half-metallic interfaces with semiconductors is still in its early stages of development.¹⁹ For the purpose of this work, we shall assume some reasonable material parameters for HMF to be used for our theoretical calculations. Heusler alloys of type $X\text{-MnSb}$ have minority spin bands with energy gap ranging from 0.5 to 1 eV.¹⁹ Therefore, we assumed that the HMF's minority spin band energy minimum to be 0.4 eV above the metal Fermi energy. This value coincides with that of NiMnSb (Ref. 20) based on a first-principle calculation. The metallic nature of HFM is due to the electronic states occupying a large energy bandwidth E_w , which is the energy of the conduction band minimum of majority spin band from Fermi energy. In this work, we arbitrarily set the metal's occupied bandwidth to $E_w = 2$ eV. We also assumed that the majority and minority spin bands in HFM has the same transport mass as Si. The choice of different transport mass in HMF would essentially introduce more reflections at the interfaces, which can also be compensated by a larger E_w . However, in the general case (e.g., Fe), the minority and majority spin bands have to be modeled differently.³⁷

The current-voltage characteristics of spin-MOSFETs for the case of parallel and antiparallel magnetization configurations in the coherent regime are plotted in Figure 2(a) and 2(b), respectively. They exhibit similar current-voltage characteristics, except that the antiparallel magnetization configurations exhibits a drain offset voltage by an amount of $\Delta_s - E_w$. This is due to the potential blockade of the majority spin at the drain HMF contact in the antiparallel configuration [see Fig. 3(b)]. Figure 3 is an intensity plot of the majority carrier density of spin MOSFETs for the case of parallel and antiparallel magnetization configurations. Also shown in Fig. 3 is the energy-resolved current (on the left). Oscillations in the energy resolved current for the parallel case are signatures of tunneling through a barrier, e.g., commonly observed in a Fowler Nordheim tunneling through Si/SiO₂/Si sandwiched structure.³⁸ In the antiparallel case [Fig. 3(b)], the potential barrier at the drain HMF contact permits transmission of the majority spin only when carrier energy is greater than Δ_s . Resonance states due to lateral confinement are observed when the carrier energy is less than Δ_s , and these states will not contribute any current.

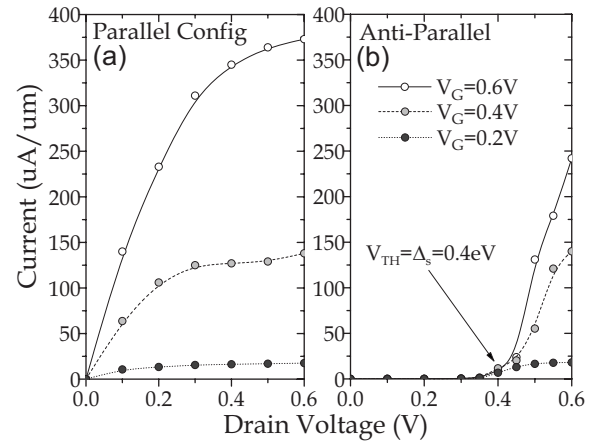


FIG. 2. (a) Current-voltage characteristics for spin MOSFET with the contacts magnetization in parallel configuration plotted for $V_G = 0.2, 0.4$, and 0.6 V. (b) Current-voltage characteristics for spin MOSFET with the contacts magnetization in antiparallel configuration plotted for $V_G = 0.2, 0.4$, and 0.6 V.

These resonance states results in the oscillatory behavior in the derivatives of the potential profile in the antiparallel configuration. It is also numerically challenging to resolve these states in the energy domain due to the relatively fine linewidth in these strongly localised resonance levels, i.e., a numerical challenge faced similarly in modeling of resonant tunneling diode. A fine gridding is employed to resolve these resonance states so that the charge density can be more reliably computed.

The magnetocurrent ratio (MR) is defined to be $\text{MR} = (I_P - I_{AP})/I_{AP}$. It serves to quantify the MR difference between the parallel and antiparallel magnetization configuration states of the device. Since the device in the antiparallel state has an apparent drain offset voltage of $\Delta_s - E_w$, I_{AP} will generally be less than I_P . Figure 4 plots the MR of the spin MOSFET under different biasing conditions. The MR follow an approximately exponential relationship with V_D at a given V_G bias. We can also see that the MR begins to diminish ($\text{MR} < 10\%$) when the V_D in the antiparallel configuration

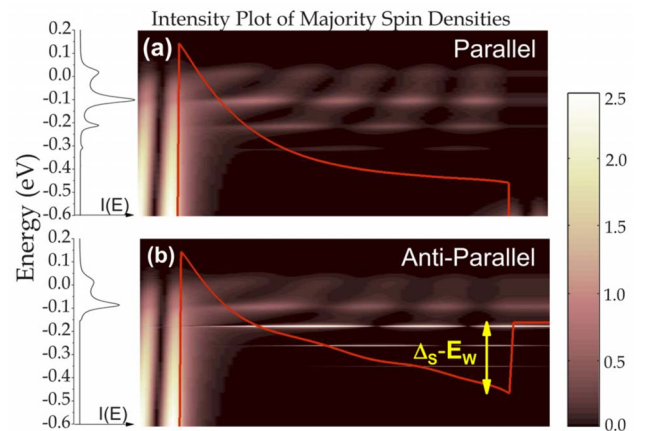


FIG. 3. (Color online) (a) Intensity plot of the majority spin density $D_u(\mathbf{r})$ (where it is scaled to present color contrast, i.e., $D_u(\mathbf{r})^{0.8}$) for the case where magnetization is in (a) parallel and (b) antiparallel configuration respectively. The terminal bias for both cases are $V_G = 0.6$ V and $V_D = 0.6$ V. The energy-resolved current is plotted to the left.

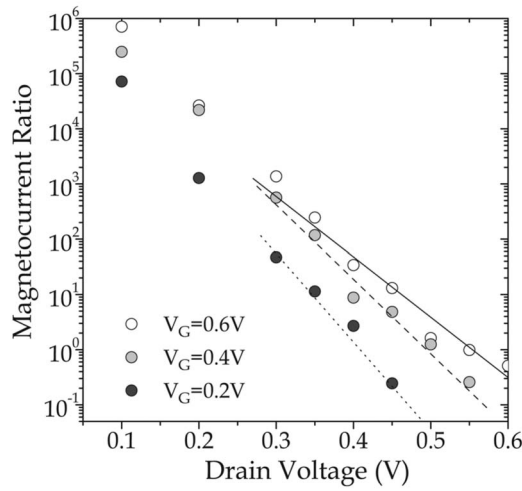


FIG. 4. MR ratio, $MR = (I_P - I_{AP})/I_{AP}$, plotted for $V_G = 0.2, 0.4$, and 0.6 V. The lines are the least square fitted to data points with $V_D \geq 0.3$ V for each V_G .

approaches the current saturation condition, i.e., $V_D = V_{sat}$. Consequently, there is a rightward shifts of the MR versus V_D curve when the gate bias V_G increases, since V_{sat} increases with increasing V_G .

IV. SPIN-MOSFET: INCOHERENT REGIME

Spin exchange scattering processes between the tunneling electron and the localized spin impurities at the HMF/Si interfaces are responsible for the incoherent nature of the electron transport. These localized spin impurities lead to decoherence of the electronic spins states. In our model, we assume that there are external reservoirs constantly maintaining these localized spin impurities in a state of equilibrium with a random polarization of spin. For a spin = 1/2 case, the completely unpolarized states corresponds to the density matrix with $F_u = F_d = 0.5$ and $\Delta = 0$.^{33,39}

As discussed in Sec. II, coupling between the number of available electrons/holes ($[G^n]/[G^p]$) for a particular state, and the in/out-flow ($[\Sigma_s^{in}]/[\Sigma_s^{out}]$) to/from that state is related through a four-index scattering tensors Φ . The scattering strength γa is assumed to be energy independent. It is proportional to n_i , the impurity concentration and to $\langle J^2 \rangle$, the averaged interaction energy of the impurity layer (see Appendix A). These parameters can be mapped to available experimental data, and they are the only parameters used to characterize the spin relaxation of the impurity layer. Figure 5(a) shows the spin polarization P in the channel due to spin injection from a HMF contact into a long-channel semiconductor. P is defined as

$$P = \frac{I_{\uparrow} - I_{\downarrow}}{I_{\uparrow} + I_{\downarrow}}. \quad (21)$$

Our model is capable of capturing the nonideal spin injection of a HMF due to the presence of a magnetically dead layer by tuning the value of γa [see Fig. 5(a)]. The spin polarization in the channel decreases with the increase of spin relaxation strength in an approximately linear fashion.

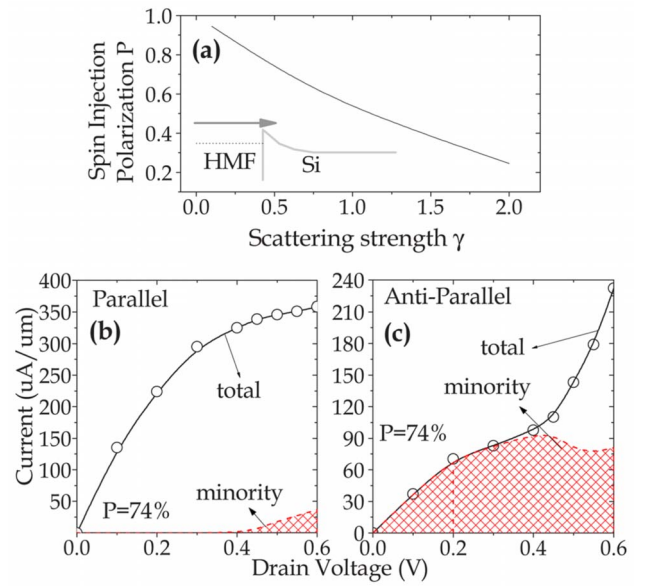


FIG. 5. (Color online) (a) Spin polarization P in the channel as a function of the interface scattering strength characterized by γa , for spin injection through a SB in a HMF/Si structure. (b) Current-voltage characteristics for spin MOSFET with the contacts magnetization in parallel configuration plotted for $V_G = 0.6$ V. All spin currents are measured at the drain. (c) Current-voltage characteristics for spin-MOSFET with the contacts magnetization in antiparallel configuration plotted for $V_G = 0.6$ V. For both cases, the spin relaxation strength at the HMF/semiconductor interfaces on both the detector and injector sides are characterized by $\gamma a = 0.5$ eV² nm. The minority spin current is plotted as dashed curve.

Figures 5(b) and 5(c) plots the drain current versus drain voltages at $V_G = 0.6$ V for both the parallel and antiparallel configuration, in the presence of spin relaxation at the HMF/semiconductor interfaces on both the detector and injector sides, characterized by spin relaxation strength of $\gamma a = 0.5$ eV² nm. In contrast to the current-voltage characteristics in the coherent case (see Fig. 2), the minority spin can now contribute to spin current, which significantly modifies the current-voltage characteristics in the antiparallel configuration. This “leakage current” is facilitated through spin relaxation at the HMF/semiconductor interfaces. Spin relaxation renders the blocking (due to the potential barrier at the drain HMF) of the majority spin transmission ineffective. Majority carriers injected from the source can now undergo spin relaxation at the HMF/semiconductor interface at the drain side and become a minority spin. Therefore, substantial amount of minority spin current is registered in the antiparallel configuration even when the drain bias is less than $\Delta_s - E_w$.

Figures 6(a)–6(d) plots the majority and minority spin densities in the parallel and antiparallel configuration at $V_G = V_D = 0.6$ V. Their respective energy resolved current is plotted in Figs. 7 and 8. In this set of calculations, the minority spin density is approximately an order of magnitude smaller than the majority spin density. In the intensity plot for the minority spin density, we observe signatures of spin-flip process at the spin injector interface as a layer of high intensity minority spins. Majority spin was scattered into the minority spin states in the injector as evanescent states with finite probability to tunnel through the SB into the channel. There-

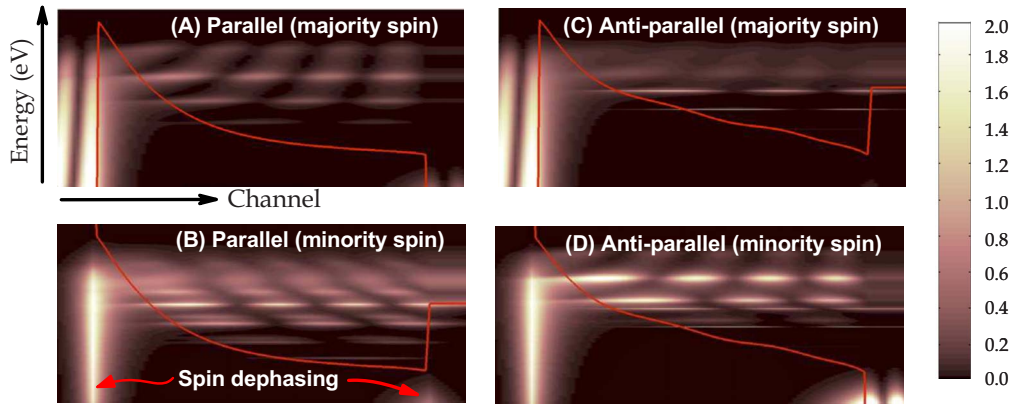


FIG. 6. (Color online) Intensity plot of the (a) majority spin density $n_u(\vec{r})$ and (b) minority spin density $n_d(\vec{r})$ (where it is scaled to present color contrast, i.e., $n_u(\vec{r})^{0.8}$ and $10 \times n_d(\vec{r})^{0.8}$, respectively) for the case where magnetization is in parallel. Similar plots for the majority and minority spin density for the antiparallel configuration in (c) and (d), respectively. The terminal bias for both cases are $V_G = V_D = 0.6$ V.

fore, HMF will not have perfect spin injection efficiency when spin relaxation mechanisms are incorporated into the model.

Figures 7 and 8 plots the corresponding energy-resolved spin current density in each of the respective device regions, i.e., (a) source, (b) channel, and (c) drain, when the device is in the parallel and antiparallel magnetization state, respectively. Although the spin current is not conserved across the device, the charge current at each energy is conserved, i.e., a property ensured by virtue of the self-consistent Born framework. From the energy resolved spin current characteristics, we can make the observation that more minority spin current is produced in the antiparallel configuration than its parallel counterpart. The energy resolved minority spin current in the antiparallel configuration is characterized by multiple resonance peaks. This is in part due to the laterally confined majority spins in the channel where the minority spin current was derived from it through spin relaxation processes.

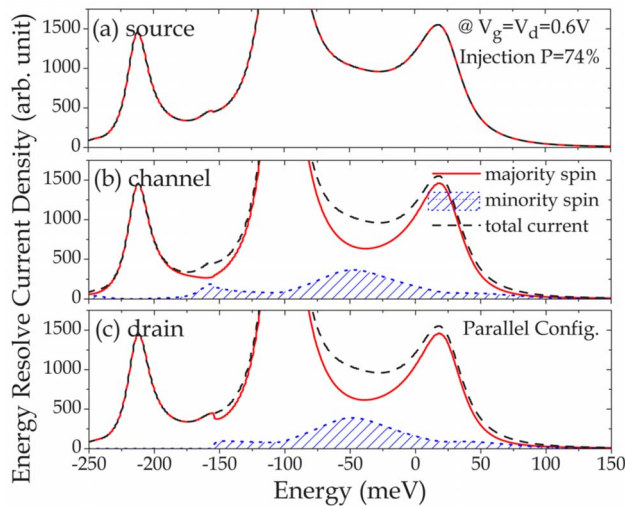


FIG. 7. (Color online) Spin current spectral density vs carrier energy, for the parallel directions of magnetization of source and drain. Total current-black dashed line, majority spin-red solid line, majority spin-blue shaded area. Top plot-at the source, middle-plot-in the center of the channel, bottom plot-at the drain.

V. INFLUENCE OF SPIN RELAXATION ON MR RATIO

In this section, we discuss MR ratio in the presence of spin relaxation. Figure 9(a) shows the MR ratio versus the drain voltage bias at $V_G = 0.6$ V in the presence of spin relaxation at the HMF/semiconductor interfaces on both the detector and injector sides, characterized by spin relaxation strength of $\gamma a = 0 - 1$ eV² nm. As evident in Fig. 9(a), the increasing spin relaxation strength at the HMF/semiconductor interfaces results in decreasing MR ratio over the whole drain voltages sweep, especially for drain biases less than $\Delta_s - E_w$. Spin relaxation process enhance the probability of conduction through the minority spin channel, which consequently smears the distinction between transport in the parallel and antiparallel configuration, resulting in diminishing MR ratio. Our analysis in this work focuses only on HMF contacts. The impact of interfacial spin dephasing on normal FM contacts could have intrinsically different dependence on the spin dephasing processes. In the Ohmic regime, one could model the interfacial spin dephasing process with a resistor element (r_γ) between the majority and minority spin channels at each contact interfaces. A simple electri-

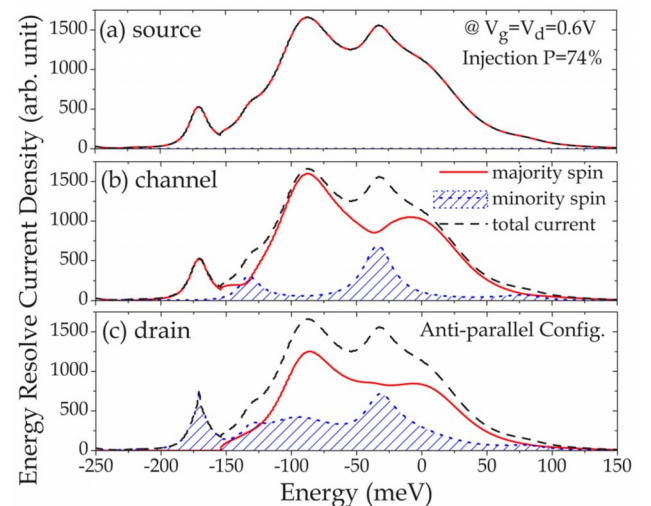


FIG. 8. (Color online) Same as in Fig. 7, for the antiparallel directions of magnetization of source and drain.

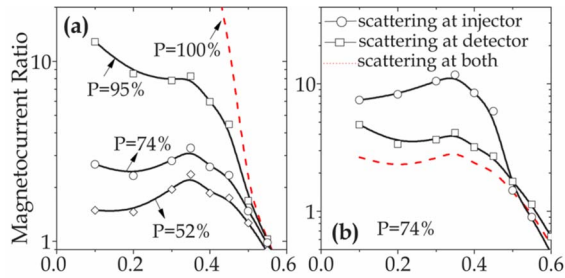


FIG. 9. (Color online) (a) MR ratio $(I_P - I_{AP})/I_{AP}$ vs drain biases for $V_G = 0.6$ V. The spin relaxation strength at the HMF/semiconductor interfaces on both the detector and injector sides are characterized by $\gamma a = 0, 0.1, 0.5$, and 1.0 $\text{eV}^2 \text{nm}$. (b) MR ratio vs drain biases for $V_G = 0.6$ V for spin relaxation at both detector and injector HMF/semiconductor interfaces (dashed line), at detector HMF/semiconductor interface only (solid line with square symbol) and at injector HMF/semiconductor interface only (solid line with circle symbol).

cal analysis of such a setup for spin-MOSFETs with either HFM or normal FM contacts shows that they have different dependence on r_γ (see Appendix B).

Lastly, we studied the impact of spin relaxation at each of HMF/semiconductor interfaces. Figure 9(b) plots the MR ratio for spin relaxation at the HMF/semiconductor interfaces at either the injector or detector side. It is evident from Fig. 9(b) that spin relaxation at the HMF/semiconductor interfaces at the detector side is more detrimental to the MR ratio than that due to the spin relaxation at the injector side, for drain bias less than $\Delta_s - E_w$. For each of these cases, Fig. 10 shows the minority spin current in the parallel and antiparallel configurations at different drain biases. As discussed previously, the fractional contribution of minority spin current in the parallel case is relatively small and arises only when the drain bias is larger than $\Delta_s - E_w$. More minority spin current is produced in the antiparallel case in this regime. From Fig. 10(b), it is evident that more minority spin current is produced when spin relaxation at the HMF/semiconductor interfaces is at the detector side compared to when it is at the injector side. The consequence is that spin relaxation at the HMF/semiconductor interfaces at the detector side is more detrimental to the MR ratio, at least for drain bias less than $\Delta_s - E_w$. A plausible explanation to why spin relaxation at the

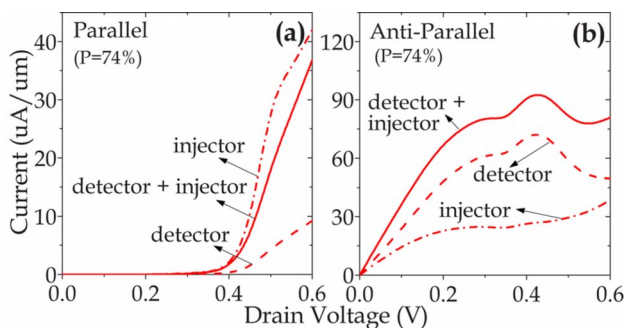


FIG. 10. (Color online) Minority spin current vs drain bias for $V_G = 0.6$ V at (a) parallel and (b) antiparallel configuration. The spin relaxation strength at the HMF/semiconductor interfaces on either/both the detector and injector sides are characterized by $\gamma a = 0.5$ $\text{eV}^2 \text{nm}$. We consider the situation where spin relaxation are at both detector and injector HMF/semiconductor interfaces (solid line), at detector HMF/semiconductor interface only (dotted line) and at injector HMF/semiconductor interface only (dash-dotted line).

detector side produces more minority spin current in antiparallel case could be understood from Fig. 6(d). When $V_D < \Delta_s - E_w$, majority carrier undergoing spin relaxation at the detector interface will either be admitted into the drain as a minority spin or be reflected back into the channel as majority spin. Waves that backscatters at the detector interface will then be reflected back and undergoes another scattering event. This multiple scattering processes enhances the spin relaxation rate. This study reveals that proper HMF/semiconductor interface treatment at the detector side is more pertinent to achieving high MR ratio in spin MOSFET for operation regime where biasing conditions is less than $\Delta_s - E_w$.

We note that a spin MOSFET uses MR caused by the change in spin transport through the device. However, in experimental realizations, a large role is played by fringe magnetic fields near the ferromagnets, which might induce local Hall effect in the semiconductor channel at vicinity of the interface. This results in a spurious contribution to the MR, as it was explained in Refs. 40–42. Measurements based on the precession of spins in the channel and the corresponding Hanle effect provide a rigorous method to detect the spin transport.^{11,12,43} Practically, one should be able to minimize this spurious Hall effect via a proper geometrical setup of the spin injection device.⁴⁴

VI. SUMMARY

In this paper, we have simulated the operation of a spin MOSFET using the NEGF approach. A large spin-splitting energy Δ_s for the HMF contacts is beneficial for achieving a large MR ratio. This is because the spin-splitting energy presents a potential barrier at the drain side in the antiparallel configuration and blocks the transmission of majority spins, resulting in a larger drain threshold voltage of $\Delta_s - E_w$ for the device in the antiparallel configuration. We highlighted and explained the bias dependence of MR ratio of spin MOSFET. Next, we demonstrated the incorporation of spin relaxation at the HMF/semiconductor interfaces via scattering self-energies. Once spin relaxation is included in the model, minority spin current arises and it dominates the leakage current in the antiparallel configuration even when the drain bias is less than $\Delta_s - E_w$. This substantially reduces the spin MOSFET MR ratio. Lastly, we studied the impact of the magnetically dead layer at the injector and at the detector sides in isolation. It was found that spin relaxation caused by the magnetically dead layer at detector side is more detrimental to the MR ratio. This can be attributed to the fact that spin relaxation due to the magnetically dead layer at the detector side is more efficient in flipping the majority spin to minority spin current.

ACKNOWLEDGMENTS

T.L. and M.S.L. gratefully acknowledge support of the Nanoelectronic Research Initiative and the Network for Computational Nanotechnology for computational resources. They also thank Sayeef Salahuddin for careful proofreading and suggestions. D.E.N. is grateful to George Bourianoff and Paolo Gargini for stimulating discussions.

APPENDIX A: DERIVATION OF SCATTERING SPIN TENSORS

In this appendix, we provide a simplified derivation and the explicit form in a particular case of spin=1/2 of the scattering tensors in Eq. (11). It follows earlier papers,^{26,33} but is presented here for completeness sake. In general, the scattering tensor is determined by the Hamiltonian of interaction with the reservoir H_I as follows:³³

$$\gamma\Phi_{ijkl}^n = \sum_{N_I} \text{Tr}[\rho H_{Iij} H_{Iik}],$$

$$\gamma\Phi_{ijkl}^p = \sum_{N_I} \text{Tr}[\rho H_{Iik} H_{Iij}], \quad (\text{A1})$$

where ρ the density matrix of the reservoir spin, like in Eq. (9), and N_I is the number of reservoir modes. In our case, the Hamiltonian (8) corresponds to the spin-spin interaction. The spin-dependent four-index tensors are thus

$$\Phi_{ijkl}^n = \text{Tr}[\rho S^\alpha S^\beta] s_{ij}^\alpha s_{ik}^\beta, \quad (\text{A2})$$

where indices α and β run over the projections of the operators on Cartesian axes, and summation over repeating index is implied.

Moreover, the prefactor contains the interaction energy J averaged over the spectral range of reservoir modes resonant with the transition (this averaging is designated by angled brackets), which according to Ref. 26 is,

$$\gamma = \sum_{N_I} J^2 \propto n_I \langle J^2 \rangle, \quad (\text{A3})$$

where n_I is the area density of impurities in the layer and averaging is done with the account of geometry of the two-dimensional layer.

For the particular case of the spins of localized electrons (reservoir) equal to 1/2, more explicit expressions can be obtained. It is convenient to use the raising and lowering Pauli matrices

$$\sigma^+ = \frac{1}{2}[\sigma^x + i\sigma^y], \quad (\text{A4})$$

$$\sigma^- = \frac{1}{2}[\sigma^x - i\sigma^y]. \quad (\text{A5})$$

The interaction Hamiltonian can be rewritten as

$$H_I = J \left[\frac{\sigma^+ S^-}{4} + \frac{\sigma^- S^+}{4} + \frac{\sigma^z S^z}{2} \right]. \quad (\text{A6})$$

It is easy to evaluate the averages of the spin operators in the state of the reservoir (9). The scattering tensor becomes

$$\Phi_{ijkl}^n = (F_u + F_d) s_{ij}^z s_{ik}^z + \Delta s_{ij}^+ s_{ik}^z - \Delta s_{ij}^z s_{ik}^+ + \Delta^* s_{ij}^- s_{ik}^z - \Delta^* s_{ij}^z s_{ik}^- + F_d s_{ij}^+ s_{ik}^- + F_u s_{ij}^- s_{ik}^+, \quad (\text{A7})$$

and similarly for Φ^p .

APPENDIX B: ELECTRICAL ANALYSIS OF HMF/FM CONTACTS IN OHMIC REGIME

The magnetocurrent ratio is an important device metric that provides a measure of the degree of distinguishability

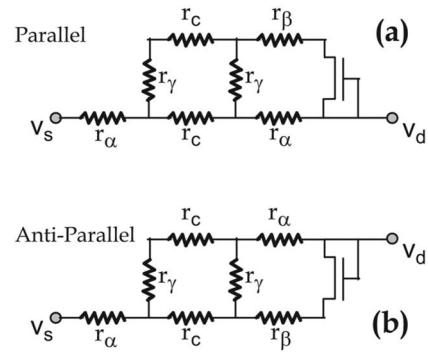


FIG. 11. (a) and (b) plot the equivalent circuit for the parallel and antiparallel configuration of a spin MOSFET in the Ohmic regime where $r_{\alpha/\beta}$ is the resistance of the majority/minority spins in the HFM contacts, r_c the channel resistance and r_γ is the resistance related to spin dephasing. The transistor switch in the equivalent circuit model has a threshold voltage of $\Delta_s - E_w$.

between the parallel and antiparallel states of the spin transistor through their measured current. The Julliere's description of the magnetocurrent ratio in terms of the available effective tunneling density of states proves to be inadequate,⁴⁵ especially when there is interfacial spin flip scattering processes. A simple analysis using the electrical circuit equivalent in Figs. 11(a) and 11(b) can offer more reliable insights.

Figures 11(a) and 11(b) plot the equivalent circuit for the parallel and antiparallel configuration in the Ohmic regime where $r_{\alpha/\beta}$ ($g_{\alpha/\beta}$) is the resistance (conductance) of the majority/minority spins in the FM contacts, r_c (g_c) the channel resistance (conductance) and r_γ (g_γ) is the resistance (conductance) related to spin dephasing. The transistor in the circuit is to model the effect of the minority/majority spin blocking due to the spin exchange energy at the drain HMF in the parallel/antiparallel configuration. A simple Ohmic model can adequately explain the late turn on of the minority current in parallel configuration at $V_D = \Delta_s - E_w$, as depicted in Fig. 5. Recall that in the parallel state, no minority spin current can be detected at the HMF drain when $V_D < \Delta_s - E_w$, as the source injected states (with energy lesser than the source Fermi energy) admitted into the drain will either decay evanescently or revealed itself as resonant levels in the channel [see Fig. 6(d)]. In addition, it also explains why the minority spin current in the antiparallel configuration can leak effortlessly into the drain once the spin dephasing process opens up the minority spin channel through g_γ .

Consider the regime where the drain bias is less than $\Delta_s - E_w$, the respective resistance for the parallel and antiparallel configuration are written as

$$r_P = 2r_\alpha + \frac{1}{2} \frac{r_c(r_c + 2r_\gamma)}{r_c + r_\gamma},$$

$$r_{AP} = 2r_\alpha + \frac{1}{2}(r_c + r_\gamma), \quad (\text{B1})$$

which both converges to $2r_\alpha + r_c/2$ when the scattering is large, i.e., $r_\gamma \ll r_c$, yielding a zero magnetocurrent ratio. Maximum magnetocurrent ratio is achieved when the scattering is minimal, i.e., $r_\gamma \gg r_c$, with a large magnetocurrent

ratio of the order r_γ/r_c . We can also derive similar expressions for normal FM contacts;

$$r_P = \frac{2r_\alpha r_\beta}{r_\tau} + \frac{(2r_\gamma r_\alpha + r_\tau r_c)(2r_\gamma r_\beta + r_\tau r_c)}{r_\tau(2r_\gamma r_\beta + r_\tau r_c) + r_\tau(2r_\gamma r_\alpha + r_\tau r_c)},$$

$$r_{AP} = \frac{2r_\alpha r_\beta}{r_\tau} + \frac{r_\gamma(r_\alpha + r_\beta) + r_\tau r_c}{2r_\tau}, \quad (\text{B2})$$

where $r_\tau = r_\alpha + r_\beta + r_\gamma$. By making the assumption that the $r_c \ll r_\gamma$, we arrive at the result that the magnetocurrent ratio for the HMF and FM case varies with the spin dephasing conductance g_γ according to g_γ^{-1} and g_γ^{-2} under these limiting conditions, respectively. This simple analysis illustrates that the impact of interfacial spin relaxation might have a different impact on the FM case.

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³⁴The matrix elements of $M^{-1}(\mathbf{r})$ are $[M^{-1}]_{11} = m_x^{-1}(\mathbf{r})$, $[M^{-1}]_{12} = m_{xz}^{-1}(\mathbf{r})$, $[M^{-1}]_{21} = m_{zx}^{-1}(\mathbf{r})$ and $[M^{-1}]_{22} = m_z^{-1}(\mathbf{r})$. In this work, we set $m_{xz}(\mathbf{r}) = m_{zx}(\mathbf{r}) = 0$.

³⁵It is also theoretically possible to further decouple the Hamiltonian H into two 1D problem when $V(\mathbf{r})$ can be written as $V(\mathbf{r}) = V_1(x) + V_2(z)$, (Ref. 46) commonly referred to as the mode space approach. When the film thickness (T_b) is sufficiently thin, i.e., < 3 nm for Si, the mode space approach is relatively accurate.

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